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Status of the Gribov–Pontecorvo Solution to the Solar Neutrino Problem

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Abstract

We discuss the status of the Gribov–Pontecorvo (GP) solution to the solar neutrino problem. This solution naturally appears in bimaximal neutrino mixing and reduces the solar and atmospheric neutrino problems to vacuum oscillations of three active neutrinos. The GP solution predicts an energy-independent suppression of the solar neutrino flux. It is disfavoured by the rate of the Homestake detector, but its statistical significance greatly improves, when the chlorine rate and the boron neutrino flux are slightly rescaled, and when the Super-Kamiokande neutrino spectrum is included in the analysis. Our results show that rescaling of the chlorine signal by only 10% is sufficient for the GP solution to exist, if the boron–neutrino flux is taken 10 – 20% lower than the SSM prediction. The regions allowed for the GP solution in the parameter space are found and observational signatures of this solution are discussed.

I. INTRODUCTION

Vacuum oscillations of maximally mixed ν_μ and ν_τ neutrinos with $(\Delta m^2)_{\text{atm}} \sim 3 \times 10^{-3} \text{ eV}^2$ are the favourite explanation of the atmospheric neutrino anomaly. A natural generalization is bimaximal mixing [1]– [10] of three active neutrinos, when mixing is described by the following matrix:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{\sqrt{2}} \\ \frac{1}{2} & \frac{1}{2} & -\frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}. \quad (1)$$

In the case of the mixing matrix given by Eq. (1), the solar neutrino oscillation is also maximal. To see this, it should be noted from Eq. (1) that

$$\frac{1}{\sqrt{2}}(\nu_\mu - \nu_\tau) = \nu_3, \quad (2)$$

while the other orthogonal combination of these states can be considered as a new field

$$\nu' = \frac{1}{\sqrt{2}}(\nu_\mu + \nu_\tau). \quad (3)$$

Using the above equations, one obtains

$$\begin{pmatrix} \nu_e \\ \nu' \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & 0 \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}. \quad (4)$$

From Eq. (4) it follows that ν_e and $\nu' = 1/\sqrt{2}(\nu_\mu + \nu_\tau)$ are a maximally mixed pair, and the flavour eigenstate ν_e is oscillating on the way from the Sun into ν' , the coherent mixture of ν_μ and ν_τ .

The above exercise is relevant to the Gribov–Pontecorvo (GP) [11] solution of the solar neutrino problem combined with atmospheric ν_μ – ν_τ oscillations. Following [11], the definition of the GP solution can be given by two conditions: (i) smallness of the oscillation length l_ν with respect to the mean distance between the Sun and the Earth $\langle r \rangle = L$

$$l_\nu = \frac{4\pi E}{\Delta m^2} \ll L = 1.5 \times 10^{13} \text{ cm}, \quad (5)$$

and (ii) smallness of the matter corrections (MSW [19]) in the Sun and in the Earth [20] (in Ref. [11] only vacuum oscillation is considered).

Indeed, in this case the averaged survival probability for ν_e is

$$\langle P_{ee} \rangle = 1 - \sin^2 2\theta \langle \sin^2 \frac{\Delta m^2 r}{4E} \rangle = 1 - \frac{1}{2} \sin^2 2\theta \equiv P_{\text{GP}}, \quad (6)$$

and from comparison with experimental data, $P_{ee} \sim 0.5$, we come to $\theta \sim \pi/4$, or to bimaximal mixing if $\nu_\mu \leftrightarrow \nu_\tau$ explains atmospheric neutrino oscillations.

Three remarks are immediately in order.

(i) There is no theoretical reason for bimaximal mixing to be exact, and more generally one should consider *near-bimaximal mixing* [1,18].

(ii) The smallness of the matter correction effects, which we included in the definition of the GP solution is actually not needed in the case of near-bimaximal mixing if only matter effects in the Sun are included. For the exact maximal mixing, $\nu_e \rightarrow \nu'$ conversion in the Sun does not change the total survival probability $\langle P_{ee} \rangle$ at the surface of the Earth [15,9]. In the arbitrary case where the mixing between ν_e and ν' is described by the mixing angle θ , and the MSW effect in the Sun converts ν_e into $\nu_S = \cos \theta_S \nu_1 + \sin \theta_S \nu_2$ (subscript S here refers

to the surface of the Sun), the total survival probability $\langle P_{ee} \rangle = |\langle \nu_E | \nu_e \rangle|^2$ on the surface of the Earth can be readily calculated as

$$\langle P_{ee} \rangle = \cos^2 \theta_S \cos^2 \theta + \sin^2 \theta_S \sin^2 \theta \quad (7)$$

For exact bimaximal mixing $\cos^2 \theta = \sin^2 \theta = 1/2$, survival probability $\langle P_{ee} \rangle = 1/2$ and thus it does not depend on θ_S , i.e. on how ν_e is converted in the Sun. For near-bimaximal mixing, Eq. (7) determines a narrow range of θ near $\pi/4$, where $\langle P_{ee} \rangle$ is practically energy independent, i.e. it does not depend on θ_S . The matter effect in the Earth, however, changes this conclusion as we shall see in the next section.

(iii) The observational data (see Fig. 1) do not support $\langle P_{ee} \rangle$ being exactly energy-independent. While the recent Super-Kamiokande (SK) data agree well with $\langle P_{ee} \rangle$ being an energy-independent constant in the energy interval 5 – 14 MeV, the values $\langle P_{ee} \rangle$ from three different experiments, GALLEX–GNO/SAGE, Homestake and Kamiokande/SK, are not exactly the same.

The aim of this paper is to discuss quantitatively the status of the GP solution. An interesting region in the parameter space is given by $\Delta m^2 \lesssim 10^{-3} \text{ eV}^2$ and $\theta \sim \pi/4$, where bimaximal mixing is characterized by $(\Delta m^2)_{\text{atm}}$ and $(\Delta m^2)_{\text{sol}}$ not very different from each other, and where the MSW effect is allowed as a small correction.

Oscillations with energy-independent suppression were suggested and studied in many works before [12–16] and most notably in the recent work of Ref. [17]. In all these works the authors have realized that the observed rate in the chlorine experiment (Homestake [25]) contradicts the energy-independent suppression, and it has to be taken larger than the observed one for it to work. In this paper we argue that 10% excess could be sufficient. Note, that the solution with energy-independent suppression is more general than the GP solution, because in the latter $l_\nu \ll L$ is assumed, while the energy-(quasi)independent solution might appear in some other regions of the parameter space.

II. PARAMETER SPACE REGIONS FOR THE GP SOLUTION

In this section we shall calculate the regions allowed for the GP solution in the parameter space $\Delta m^2, \tan^2 \theta$. We first define the oscillation parameter space where the solar neutrino survival probability behaves effectively as the GP one. In order to do so we impose the condition that for any of the i solar neutrino fluxes (integrated over the different production point distributions) the survival probability in the relevant range of energies does not differ by more than 10% (1%) from P_{GP} given by Eq. (6):

$$\frac{|P_{ee}^i(E/\Delta m^2, \theta) - P_{\text{GP}}(\theta)|}{P_{\text{GP}}(\theta)} < 0.1 \text{ (0.01)} \quad \text{for } E_{i,\text{max}} > E > E_{i,\text{min}}, \quad (8)$$

where $E_{i,\text{max}}$ and $E_{i,\text{min}}$ determine the range of energies in which the flux i is detected in present experiments. For instance, for $i = pp$, $E_{pp,\text{min}} = 0.233 \text{ MeV}$ and $E_{pp,\text{max}} = 0.42 \text{ MeV}$. In the evaluation of the corresponding survival probabilities, we have included the matter

effects when propagating in the Sun and in the Earth as well as the distance interference term:

$$P_{ee}^i = P_{e,1}^S P_{1,e}^E + P_{e,2}^S P_{2,e}^E + 2\sqrt{P_{e,1}^S P_{e,2}^S P_{1,e}^E P_{2,e}^E} \cos \frac{\Delta m_{21}^2(L)}{2E}, \quad (9)$$

where $P_{e,i}^S$ is the probability for the ν_e to exit the Sun in the mass eigenstate i , while $P_{i,e}^E$ is the probability for the mass eigenstate i arriving at the Earth to reach the detector as a ν_e . L is the average distance between the Sun and the Earth.

In Fig. 2 we show the parameter space $\Delta m^2, \tan^2 \theta$ where the condition given by Eq. (8) is verified at 10% (lighter shadow) and 1% (darker shadow). The only interesting sector of the effective-GP region in this parameter space is located at large Δm^2 around the maximal mixing line $\tan^2 \theta = 1$, where matter effects in the Sun are suppressed. This region is limited from above by the CHOOZ reactor data [27]. Only in this sector there is an overlap with the rate- and spectra-allowed regions (see below).

As was discussed above, for maximal mixing the matter effects in the Sun do not alter the energy-independent survival probability P_{ee} on the way from the production point inside the Sun to the surface of the Earth. However Earth matter effects make P_{ee} energy-dependent in the regions of maximal mixing at $10^{-5} \lesssim \Delta m^2 \lesssim 10^{-8}$. In contrast with our calculations, the region $\Delta m^2 \lesssim 10^{-7}$ is found in ref. [17] as energy-independent one. We explain this discrepancy by two effects:

- For $10^{-8} \lesssim \Delta m^2 \lesssim 10^{-7}$ Earth matter effects for pp -neutrinos result into an energy dependence of the survival probability beyond 10%.
- At $\Delta m^2 \lesssim 10^{-8}$ the L dependent interference term in Eq. (9) gives strong energy dependence of the ${}^8\text{B}$ flux. This term was not included in the calculations of Ref. [17].

As we mentioned above, the GP solution is incompatible with the central value of the rate measured by the Homestake detector $R_{\text{Cl}} = 2.56$ SNU [25]. Following the prescription of many works, we shall use the rescaled rate $R_{\text{Cl}}^{\text{res}} = 2.56 f_{\text{Cl}}$ SNU, assuming $f_{\text{Cl}} \gtrsim 1$ to be a free parameter. In Fig. 3 we plot the χ^2 function from the analysis of the three observed rates as a function of the f_{Cl} factor for different constant values of the survival probability $P_{\text{GP}} = 0.5, 0.59$ and 0.71 . The upper left panel corresponds to oscillations into active neutrinos while the lower one into sterile neutrinos. The differences between these two scenarios arise from the absence of NC contribution to the SK rate in case of oscillations into sterile neutrinos. From this figure we see that the best GP-like solution corresponds to survival probability slightly larger than that for maximal-mixing case (close to 0.59) both for active and sterile neutrinos. The quality of these solutions are considerably improved when allowing a 30–50 % increase in f_{Cl} . This improvement is more significant for the case of sterile neutrinos since the corresponding survival probability at SK agrees better with the data from gallium detectors (see Fig.1).

This behaviour is also illustrated in Fig. 4 where we show the $\Delta m^2, \tan^2 \theta$ regions allowed by the statistical analysis of the rates of GALLEX–GNO/SAGE [22,23,21], SK [24] and Chlorine [25] experiments for different values of f_{Cl} in case of active and sterile neutrinos,

and for Bahcall-Pinsonneault (BP00) [26] fluxes. The solutions, following the standard statistical analysis (for details see Ref. [28]), are shown at 99% CL. The effective GP solutions are marked as dark areas. Notice that they appear at $f_{\text{Cl}} \gtrsim 1.1$ (1.2) for active (sterile) oscillations and that all regions displayed have a cut at $\Delta m^2 \approx 8 \times 10^{-4}$ as a consequence of the CHOOZ [27] bound.

Inclusion of SK data on the energy spectra of boron neutrinos improves the quality of the GP solution. In Fig. 5 we display, for different values of f_{Cl} , the regions allowed by the analysis of the rates and day–night spectrum of boron neutrinos measured by SK [24]. Again the solutions are shown at 99% CL and the effective GP solutions are marked as dark areas. From these figures one can see that the inclusion of the spectra data results in the appearance of allowed regions for the GP solutions at smaller values of f_{Cl} . This is a natural result, because the rates of GALLEX–GNO/SAGE and Homestake can be also considered as information about the solar neutrino spectrum, in its low energy part, however in contrast to the low energy part of the spectrum, the GP solution describes well the spectrum observed in SK.

In Figs. 4–5 we have used the boron neutrino flux as calculated in the Standard Solar Model [26]. This flux has a large theoretical uncertainty mostly due to uncertainties in the pBe cross-section. In order to study the effect of a possible deviation of the ^8B flux from the SSM prediction [26], we shall introduce the rescaled boron neutrino flux defined as $\Phi_{\text{B}} = f_{\text{B}} \Phi_{\text{B}}^{\text{SSM}}$ with $\Phi_{\text{B}}^{\text{SSM}}$ given by [26]. In the central panels in Fig. 3, we plot the χ^2 function from the analysis of the three observed rates as a function of f_{Cl} for different constant values of the survival probability P_{GP} when the factor f_{B} is left free. The upper central panel corresponds to oscillations into active neutrinos, the lower one into sterile neutrinos. In the right panels we show the corresponding values of f_{B} , which give the best agreement with the data for each value of f_{Cl} and P_{GP} . From this figure we find that although using a free $f_{\text{B}} < 1$ leads to a further increase of the statistical significance of the GP solution, it has a smaller impact than the corresponding variation of f_{Cl} . It, however, allows for the presence of GP solutions with smaller f_{Cl} . This is particularly the case for oscillations into active neutrinos.

In Fig. 6 we plot the allowed regions from the analysis of the rates and day–night spectrum of ^8B neutrinos measured by SK for different values of f_{Cl} and f_{B} . For the sake of concreteness we have chosen the f_{B} factor that gives a better fit to the three rates for each value of f_{Cl} for maximal mixing. Namely, f_{B} is chosen as $f_{\text{B}} \sim 0.8$ (0.9) for oscillations into active (sterile) neutrinos. In Fig. 6 the left panels correspond to oscillations into active neutrinos and the right ones into sterile neutrinos. Comparing this figure with the corresponding panels in Figs. 5 we see that lowering the ^8B normalization leads to a larger overlap between the allowed LMA region and the GP solution already for $f_{\text{Cl}} \leq 1.1$, in the case of oscillations into active neutrinos.

III. CONCLUSIONS

It could be that nature has chosen the most unsophisticated scheme of neutrino oscillations: three active neutrinos with (nearly) bimaximal mixing. Mixing of ν_{μ} and ν_{τ} explains

the atmospheric neutrino anomaly, and of ν_e and $\nu' = (1/\sqrt{2})(\nu_\mu + \nu_\tau)$ the solar neutrino deficit. In this case, the GP solution, provided by condition (5), naturally appears, and it is characterized by an energy-independent survival probability $\langle P_{ee} \rangle = P_{GP}$.

The GP solution is disfavoured by the Homestake rate, but describes well the other rates as well as the energy spectrum observed in SK. The statistical significance of the GP solution strongly improves if one assumes rescaling of the chlorine rate by a factor $f_{Cl} = 1.1\text{--}1.5$, while some further improvement arises if the 8B neutrino flux is also rescaled by a factor $f_B = 0.7\text{--}0.9$. In particular if the 8B flux happens to be 10–20% lower than the BP00-predicted central value, the GP solution for maximal mixing in active oscillations would be allowed with a chlorine rescaling factor $f_{Cl} \lesssim 1.1$.

The GP solution will be directly searched for in the KamLand experiment [29]. Detection of reactor neutrinos can result in the measurement of Δm^2 in the interval $10^{-3}\text{--}3 \times 10^{-6} \text{ eV}^2$ for large mixing angles. If Δm^2 is found outside the LMA MSW region or inside it at $\theta \approx \pi/4$, would mean the discovery of the GP solution.

In low energy solar neutrino experiments the signatures of the GP solution are the ordinary suppression of 7Be neutrinos given by a factor $P_{GP} = \frac{1}{2} \sin^2 2\theta$ and the absence of anomalous seasonal variations (beyond the geometrical ones). These features can be clearly seen in Borexino [30] and KamLand [29] experiments.

Note

This work was presented by M.C.Gonzalez-Garcia at the Gran Sasso Laboratory at the 5th Topical Workshop on “Solar Neutrinos: Where are the Oscillations?” (March 2001). On March 29 the preprint by S. Choubey, S. Coswami, N. Gupta and D.P. Roy [17] appeared in the net. The basic assumptions they used, rescaling of the chlorine and boron fluxes, are the same as in our paper, but we are considering a GP solution that is not, in principle, identical to the energy-independent solution, studied in the aforementioned paper. The most noticeable difference in our results relates to the low Δm^2 solutions found in Ref. [17] and shown in their figures 1 -4. They are not present in our solutions partly due to interference term given in our Eq.(9) and disregarded in Ref. [17].

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FIGURES

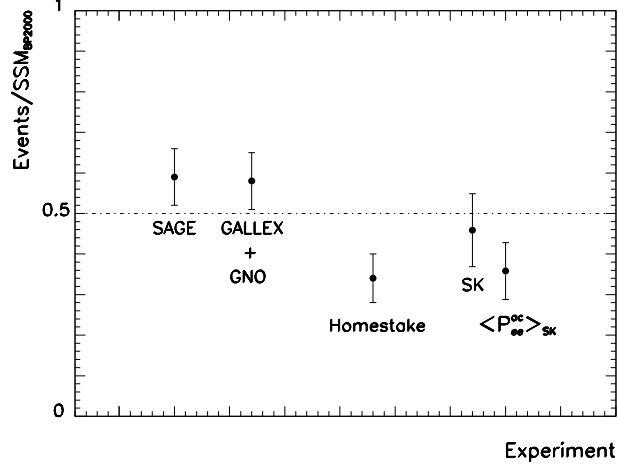


FIG. 1. Ratios of observed rates to the BP00 prediction for the existing experiments. In the case of oscillations the ratios for all experiments, except Super-Kamiokande, are equal to the ν_e survival probability P_{ee} . For Super-Kamiokande the ratio SK gives P_{ee} in the case of oscillation to sterile neutrinos, while for the case of oscillation to active neutrino we plot the corresponding $P_{ee,ac}$.

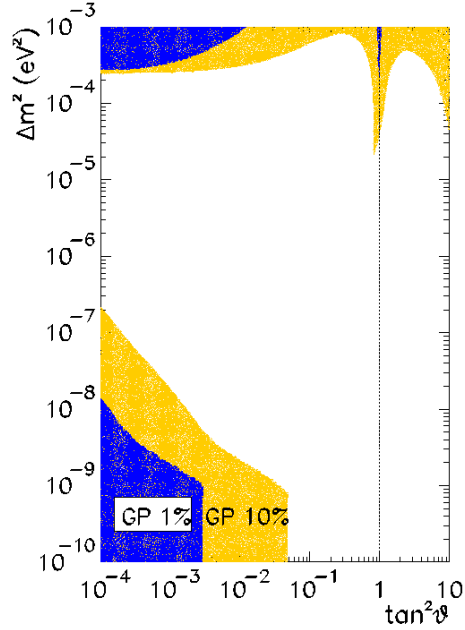


FIG. 2. Regions in Δm^2 , $\tan^2 \theta$ parameter space, where the ν_e survival probability $P_{ee}(E)$ differs from the energy-independent GP survival probability P_{GP} by less than 10% (lighter shadow) and less than 1% (dark shadow). See the text for details.

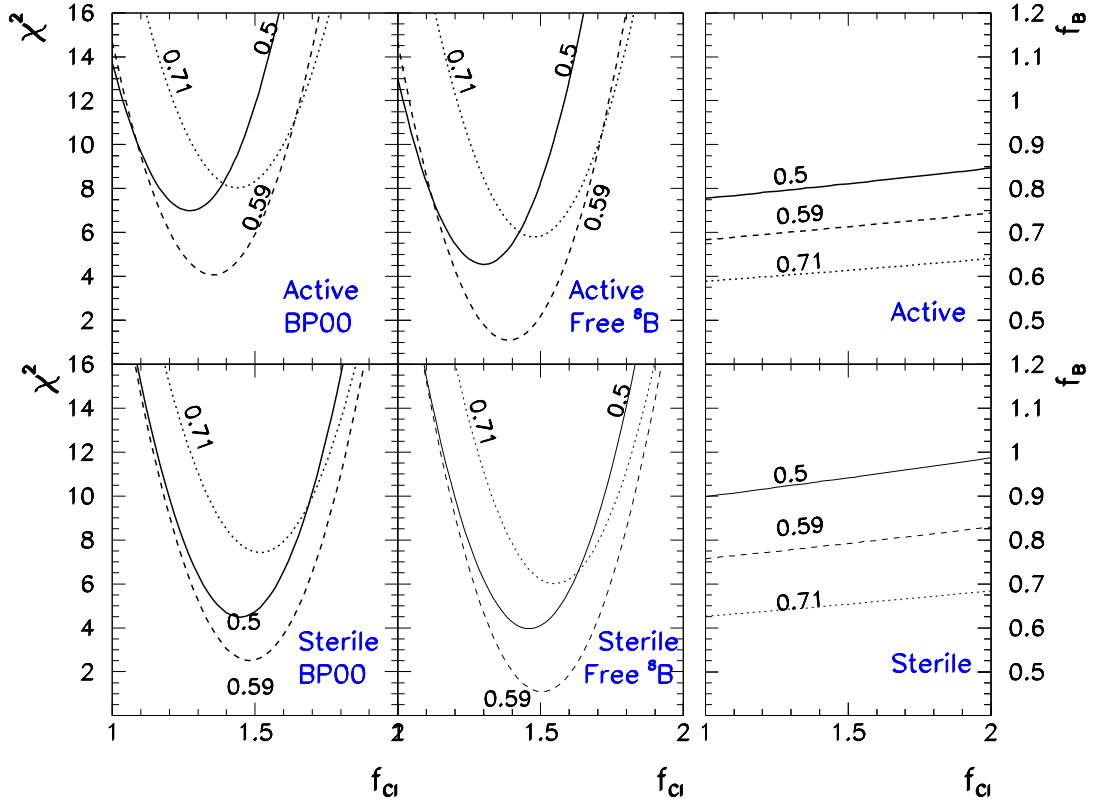


FIG. 3. χ^2 analysis of the three observed rates as a function of the f_{CI} factor for different constant values of the survival probability $P_{GP} = 0.5, 0.59$ and 0.71 (solid, dashed and dotted lines respectively). The upper (lower) panels correspond to oscillations into active (sterile) neutrinos. In the left panels we have used BP00 boron fluxes ($f_B = 1$), while in the central panels f_B is left free to optimize χ^2 . The resulting f_B values which optimize χ^2 for given f_{CI} and P_{GP} are plotted in the right panels.

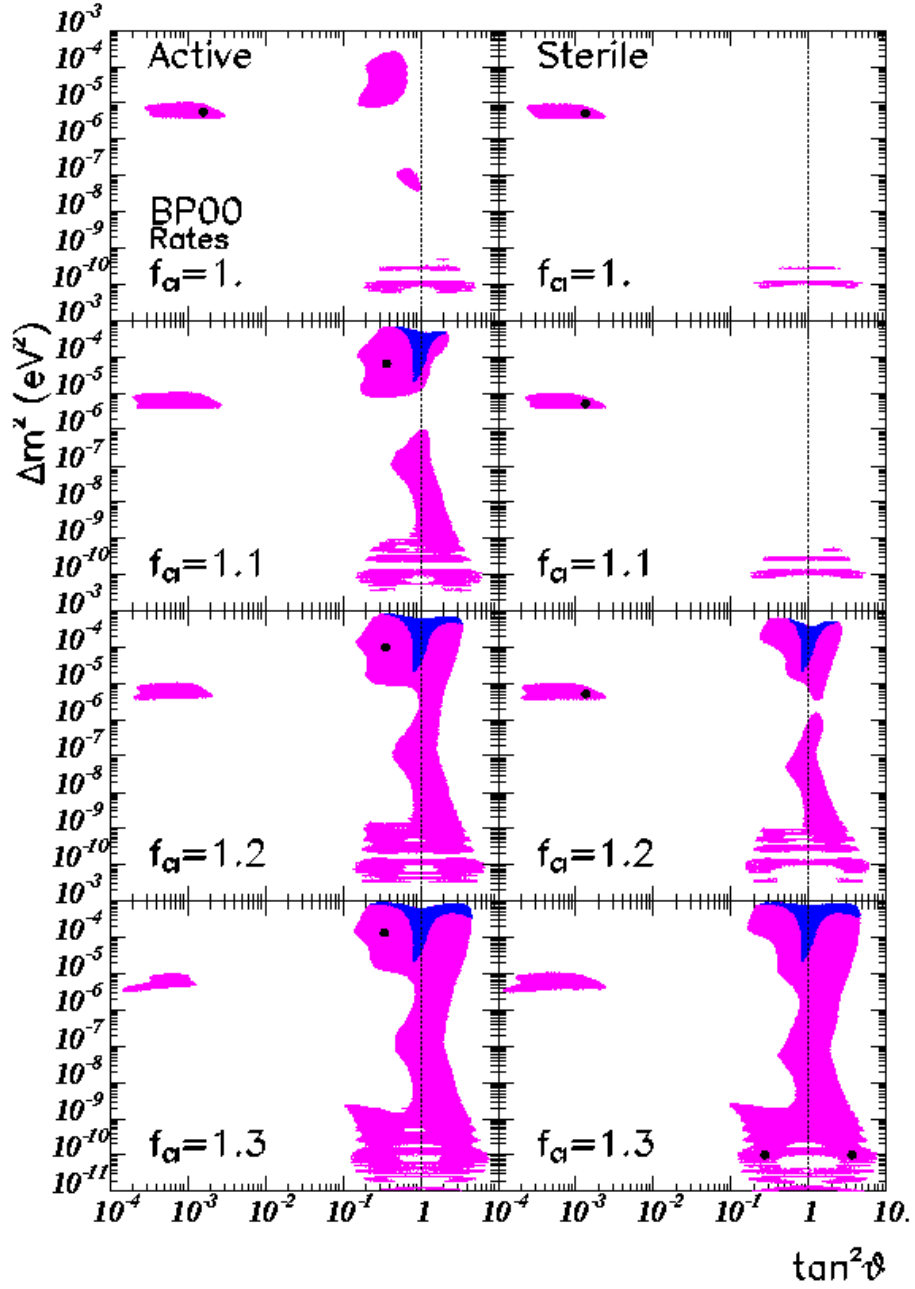


FIG. 4. 99% CL regions allowed by the analysis of the experimental rates in GALLEX–GNO/SAGE, SK and Chlorine experiments, for BP00 fluxes, for different values of f_{Cl} and for oscillations into active (left panels) and sterile (right panels) neutrinos. The dots mark the position of the best-fit points in each panel. The effective GP solutions are marked as dark areas.

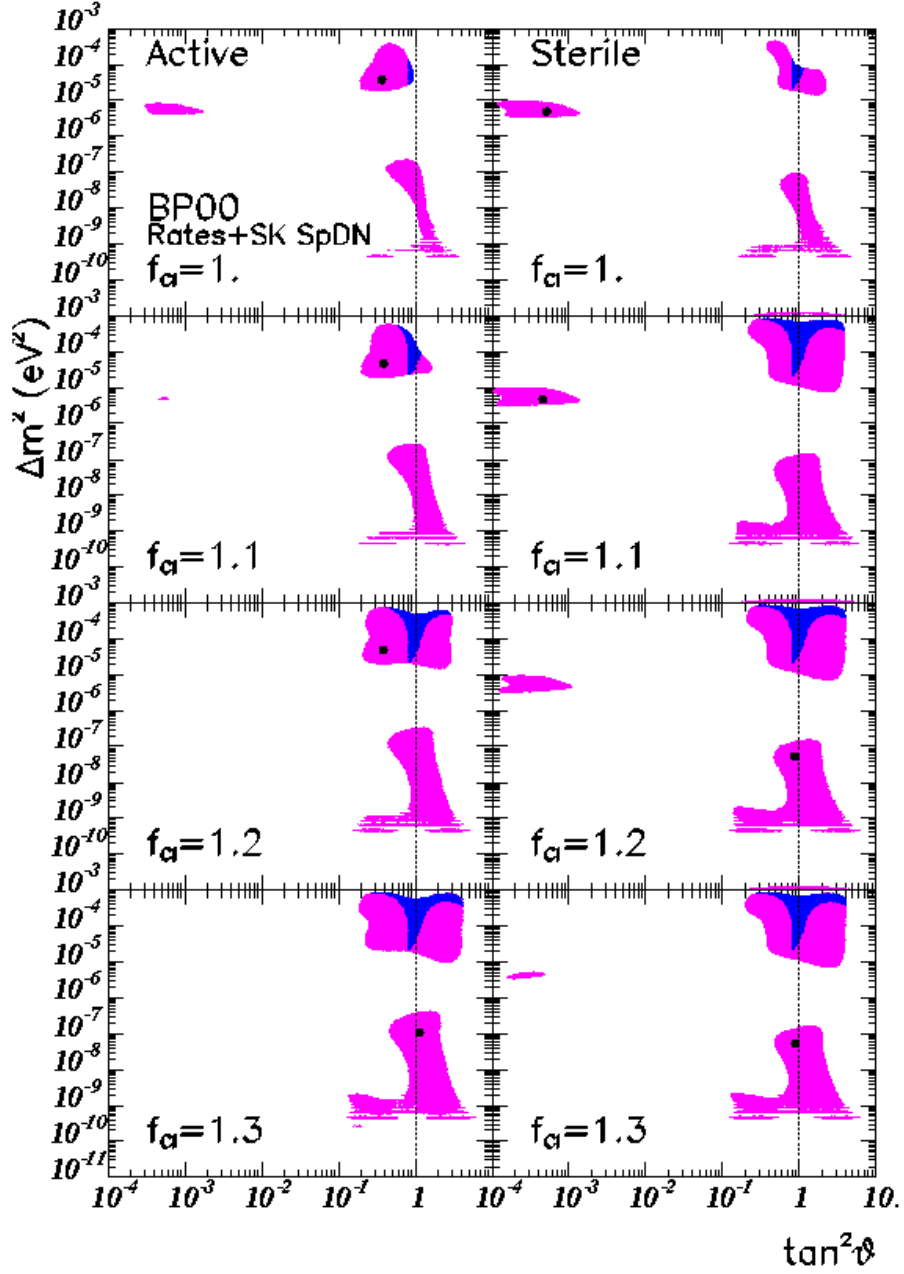


FIG. 5. 99% CL regions allowed by the analysis of the three experimental rates and the SK day–night spectrum, for BP00 fluxes, for different values of f_{α} and for oscillations into active (left panels) and sterile (right panels) neutrinos. The dots mark the position of the best-fit points in each panel. The effective GP solutions are marked as dark areas.

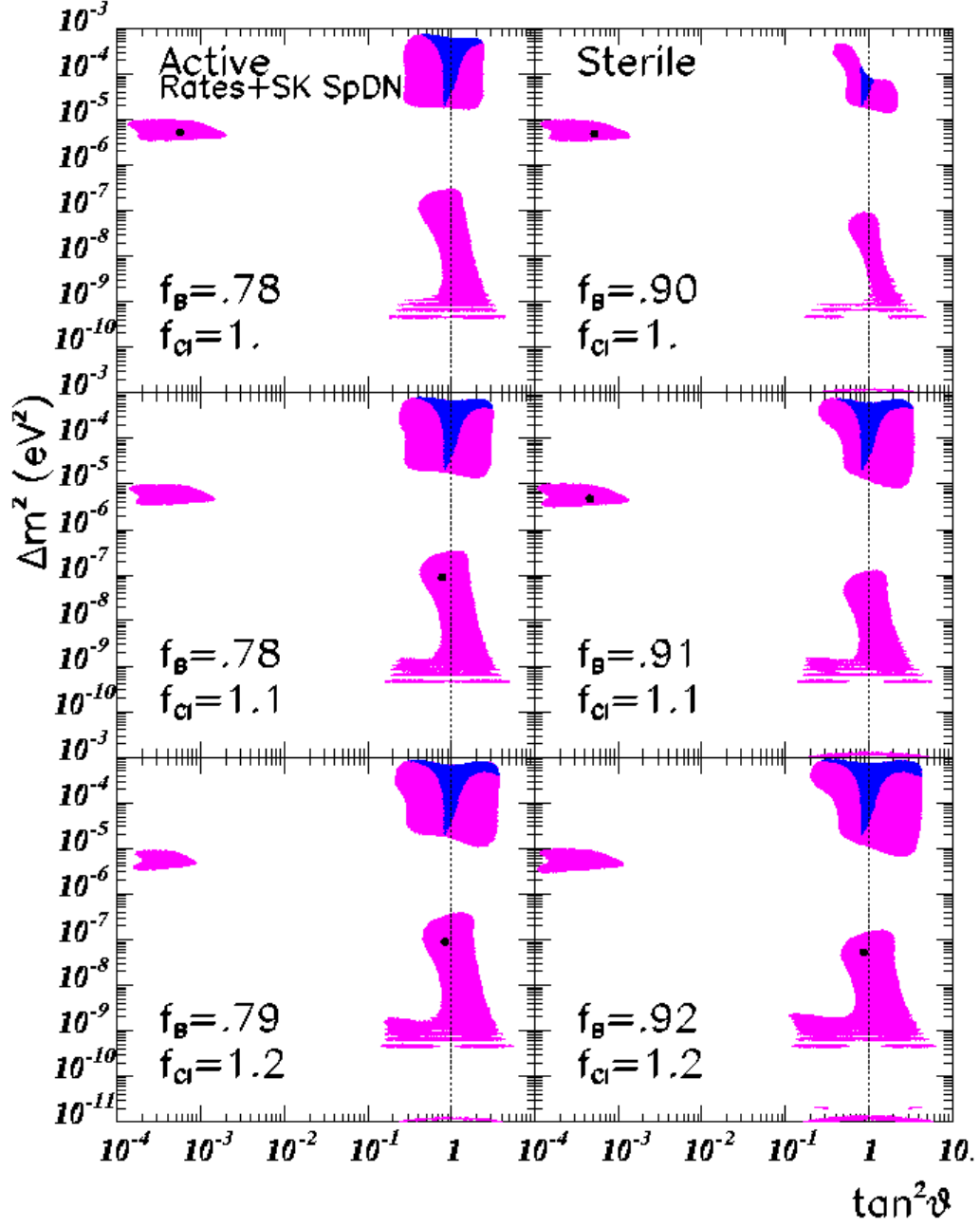


FIG. 6. 99% CL regions allowed by the analysis of the three experimental rates and the SK day–night spectra for different values of f_{CI} and f_B , for oscillations into active neutrinos (left panels) and sterile neutrinos (right panels). The effective GP solutions are marked as dark areas. The dots mark the position of the best-fit points in each panel.